

Maths

# Home Learning 

## Maths Pack

Exercises

## Week 1: Transformations

## Session 1: Translation

## Concept Corner




We say a shape has been $\qquad$ when every point in the shape moves by the same distance in the same $\qquad$ . We can use a $\qquad$ to describe the translation.
e.g. The transformation from $A$ to $B$ is a translation by the vector $\qquad$ The shape moves $\qquad$ to the right and $\qquad$ down.
1.

a) Write down the coordinates of the points A - H
b) Describe the journey using vector notation:

$$
\text { e.g. A to B: }\binom{2}{1}
$$

i) C to D
ii) D to E
iii) F to A
iv) D to C
v) E to D
vi) A to F
2. Describe the journey using vector notation:

3. Describe the transformation in each case:

a) A to B
b) B to D
c) A to D
d) A to C
e) C to D
f) D to A
4. Sketch, on a single diagram, the outcome of translating the shape by:
$\binom{2}{-2}, \quad\binom{-2}{-2}, \quad\binom{-2}{2}, \quad\binom{2}{2}, \quad\binom{4}{0}, \quad\binom{-4}{0}$
a)

b)

c)

5. Describe four translations of the octagons that sends the shapes inside the square forming a tessellation pattern.


## Questions for depth:

1. Four copies of the triangle $2 \downarrow$ are arranged as follows:
a) If $A$ is translated by $\binom{3}{2}$, $B$ is translated by $\binom{3}{-4}$ and
 C by $\binom{0}{-2}$ what quadrilateral is formed?
b) A is translated by $\binom{2}{0}$, $B$ is translated by $\binom{2}{-2}$ and C by $\binom{0}{-2}$ what quadrilateral is formed?


## Week 1 Session 2: Rotation

Concept Corner



We can $\qquad$ a shape about a point called the centre of $\qquad$ .
e.g. The transformation from A to B can be described as a rotation of $\qquad$ clockwise about the point $\qquad$ . The transformation from B to A can be described as a rotation of $\qquad$ about the same point.

1. Draw a copy of each shape after:
a) a $90^{\circ}$ rotation clockwise
b) a $180^{\circ}$ rotation
c) a $270^{\circ}$ rotation clockwise

d) a $90^{\circ}$ rotation anticlockwise
2. Generate five statements describing the angle and direction of rotation between two shapes:
 e.g. "H to C is a rotation of $270^{\circ}$ clockwise."

3. Describe the following transformations:
E.g. C to A "a rotation of $90^{\circ}$ clockwise about the origin."
a) A to B
b) $B$ to $D$
c) A to D
d) A to C
e) C to D
f) D to A

4. Describe the following transformations:
a) A to B
b) B to D
c) A to D
d) A to C
e) $C$ to $D$
f) D to A

5. Sketch, on a single diagram, the outcome of rotating the shape by $180^{\circ}$ about each of the six points:
a)

b)

c)

6. Sketch, on a single diagram, the outcome of rotating the shape by $90^{\circ}$ clockwise about each of the points:
a)

b)

c)


## Questions for depth:

1. Describe four rotations of the octagons that sends the shapes inside the square forming a tessellation pattern.


## Week 1 Session 3: Reflection

## Concept Corner




We can $\qquad$ a shape in a $\qquad$ A point and it's reflection are $\qquad$ from the line of reflection.
e.g. The transformation from A to $B$ can be described as a reflection in the line $\qquad$ . The transformation from B to C can be described as a reflection in the line $\qquad$ .

1. Identify the number of lines of symmetry:
a)

b)

c)

2. Copy the shape and reflect it in the dotted line.
a)

b)

c)

3. Write the equation for each line:

4. Describe the following transformations:

a) $A$ to $B$
b) B to D
c) A to D
d) A to C
e) C to D
f) D to A
5. Two lines $M_{1}$ and $M_{2}$ are shown. Describe the following transformations:
i) B to D
ii) $D$ to $B$
iii) A to C

6. Describe four reflections of the octagons that sends the shapes inside the square forming a tessellation pattern.

## Questions for depth:



1. Four copies of the triangle 2
 are arranged as follows:
a) Describe the transformation from B to C

b) Describe the transformation from A to D
c) Describe the transformation from A to C


## Week 1 Session 4: Isometries

## Concept Corner



Reflection, rotation and translation are all examples of isometries.
Triangle A has been $\qquad$ $90^{\circ}$ clockwise about $(3,2)$ to give triangle $\qquad$
Triangle A has been $\qquad$ in the line $x=$ $\qquad$ to give triangle $\qquad$
Triangle A has been $\qquad$ by $\binom{-4}{-2}$ to give triangle $\qquad$

1. Look at the image below. Write down single transformations to which could transform:
a) $A$ onto $R$
b) $A$ onto $P$
c) A onto Q
d) A onto $S$

2. Look at the triangles in Q 1 .
a) What single transformation could transform Q onto S ?
b) What single transformation could transform $R$ onto Q ?
3. In your book draw a set of axes where both $x$ - and $y$-axes range from $0-10$.

Copy triangle A from Q1 onto your axes.
Now, on your axes, draw the images created by the following transformations:
a) Translate A by $\binom{5}{-1}$
b) Reflect A in the line $y=5$
c) Rotate $\mathrm{A} 90^{\circ}$ clockwise about $(7,1)$
4. Look at the diagram below. Write down three different transformations that could have transformed square $X$ onto square $Y$.

5. Look at the image below. Do you agree with Rosie's statement? Explain your answer.


## Questions for depth:

1. Explore the different transformations that takes one square to another in the following image:


## Week 2: More transformations

## Session 1: Combining reflections

## Concept Corner

A combination of $\qquad$ can sometimes be described by a different single transformation. e.g. Triangle A is reflected in the line $M_{1}$ to give $\qquad$ $\ldots$.
$\mathrm{A}^{\prime}$ is then $\qquad$ in the line $M_{2}$ to give $\qquad$ .

A could also be mapped to $A^{\prime \prime}$ by a translation by the vector $\qquad$ _.


1. For each question:
a) Reflect A and B in line $M_{1}$ followed by $M_{2}$. Label the results A' and $\mathrm{B}^{\prime}$.
b) Reflect A and B in line $M_{2}$ followed by $M_{1}$. Label the results $\mathrm{A}^{\prime \prime}$ and $\mathrm{B}^{\prime \prime}$.
c) Find a translation that would map A to A', A to A", B to B' and B to B".
i)

ii)

ii)

2. a) Give the translation that maps A to $\mathrm{A}^{\prime}$ ?
b) Find the equation of two possible mirror lines that would reflect triangle A to A'.
c) Find another three examples of two mirror lines that would map A to A'. What do all the pairs have in common?

3. For each question:
a) Reflect A line $M_{1}$ followed by $M_{2}$. Label the results A'.
b) Find a translation that would map A to A'.
c) Describe the relationship between this translation and the lines $M_{1}$ and $M_{2}$.
i)

ii)

iii)

4. Sam tries reflecting the triangle $A$ in a vertical and then a horizontal line. He notices that if he reflects in these lines in either order, the triangle ends up in the same position.

How is this different to when the two lines are parallel?

Does this always work if the two lines of reflection are perpendicular?



## Questions for depth:

1. 

a) Reflect A line $M_{1}$ followed by $M_{2}$. Label the results
b) What transformation would map A to $A^{\prime}$
c) Try moving A to a different position. What do you notice?
d) How does this transformation relate to the lines $M_{1}$ and $M_{2}$.


## Week 2 Session 2: Combining translations and reflections

## Concept Corner



We can combine a translation and a reflection by performing one $\qquad$ after the other. For example: A is translated by the vector $\qquad$ to give $\mathrm{A}^{\prime}$. $\mathrm{A}^{\prime}$ is then ___ in the line $\qquad$ to give A".
1.
a) What are the co-ordinates of the vertices of this triangle?
b) State the co-ordinates of the vertices of the translated shape:

i) A translation by the vector $\binom{2}{0}$
ii) A translation by the vector $\binom{0}{-3}$
iii) A translation by the vector $\binom{1}{1}$
iv) A translation by the vector $\binom{-2}{2}$
2. State the co-ordinates of the reflected triangle:

3. A student is exploring the effect of combining a translation and a reflection.


Reflect in the dotted line

Translate by the vector $\binom{-2}{2}$


The order in which I reflect and translate doesn't matter in this case.

$$
\begin{gathered}
\mathrm{A} \rightarrow \mathrm{~B}_{1} \rightarrow \mathrm{C} \text { or } \\
\mathrm{A} \rightarrow \mathrm{~B}_{2} \rightarrow \mathrm{C}
\end{gathered}
$$

4. Explore completing the two transformations in different orders:
a)

Reflect in the dotted line
b)

Translate by the vector $\binom{1}{1}$
c)

Reflect in the dotted line
Translate by the vector $\binom{2}{0}$
d)

Translate by the vector $\binom{0}{-3}$
Translate by the vector $\binom{2}{-2}$

## Questions for depth:

1. How far apart are the two options?

Option 1: A shape is translated by a vector $\binom{a}{0}$ then reflected in the line $x=b$
Option 2: The same shape is reflected in the line $x=b$ then translated by a vector $\left({ }^{a}\right)$

## Week 2 Session 3: Enlargement

## Concept Corner

 .The enlarged shape will
We can enlarge shapes using a $\qquad$ -
the transformation from A to $B$ is an $\qquad$ of scale factor $\qquad$ the sides of the polygon are twice as long. The transformation from $B$ to $A$ is an enlargement of scale factor $\qquad$ the sides are ___ as long.
1.
a)

b)

c)

i) State the scale factor of enlargement for each of the following transformations from A to B
ii) State the scale factor of enlargement from $B$ to $A$
2. On squared paper draw an enlargement of each shape:
a) with a scale factor of 2
b) with a scale factor of 3

c) with a scale factor of 1

3. Find the perimeters of each of the shapes in Q1. What do you notice?
4.

Draw a sketch of the following shape after it has been enlarged by a scale factor of :
a) 2
b) $\frac{1}{2}$
c) 3

5. Find the perimeters of each of the enlarged shapes in Q4.
6.
a) The 2 by 3 rectangle below was partitioned into 4 triangles and enlarged by a scale factor of 2:


Draw a 2 by 3 rectangle on squared paper and partition it your own way, then enlarge it by a scale factor of 2 .
7. Sketch each of the following shapes on square paper and then enlarge them by a scale factor of 3 :
a)

b)

c)

d)


## Questions for depth:

1. Hexagon A is enlarged by a scale factor of $a$ and hexagon B by a scale factor of $b$. The perimeters of the two enlarged shapes are the same.
a) Suggest four possible values for $a$ and $b$
b) Write an equation linking $a$ and $b$


## Week 2 Session 4: Enlargements and area

## Concept Corner



When we $\qquad$ a shape can affect the area. There is a relationship between the scale factor and how the area $\qquad$ .The example above shows two different enlargements of the triangle on the left. If we enlarge by a $\qquad$
$\qquad$ of 2 , the area becomes $\qquad$ times greater.

1. Find the area of the following shapes:
a)

b)

c)

d)

2. 

a) Sketch each of the shapes above following an enlargement of scale factor 3
b) Find the area of the enlarged shapes, what do you notice?
3. Hassan is trying to use copies of a shape to create an enlargement. Use four copies of each shape to enlarge them by a scale factor of 2 .

I used four copies to create an enlargement of this shape with a scale factor of 2 .

a)

b)

c)

4. Rosie is comparing the area of a parallelogram before and after it has been enlarged:


$$
\text { Area }=4 \times 8 \mathrm{~cm}^{2}=32 \mathrm{~cm}^{2}
$$

$$
\text { Area }=3 \times 4 \times 3 \times 8 \mathrm{~cm}^{2}=9 \times 32 \mathrm{~cm}^{2}
$$

Use a similar strategy to show many times greater the area is following an enlargement by scale factor:
a) 5
b) 12
c) $n$
5. A map of an island is drawn on a square centimetre grid. The actual island is an enlargement of the map by a scale factor of approximately 2000000 .

a) Estimate the length of the coast line.
b) Estimate the area of land of the island.

## Questions for depth:

1. Three circles of radius $1 \mathrm{~cm}, 2 \mathrm{~cm}$ and 6 cm sit inside a larger circle. The four centres lie on the same horizontal line. Compare the area of the smallest circle to the three larger circles. How many times greater are they?


## Week 3: Prime factorisation 1

## Session 1: Indices

## Concept Corner



When numbers are written "to the power of" it is called $\qquad$ notation. So $5 \times 5$ can be written as $5^{2}$, and is said ' 5 to the power of 2 ', or ' 5 $\qquad$ '. $6 \times 6 \times 6 \times 6$ can be written as $6^{4}$, and is called 6 to the power of $\qquad$ .

Diagram A shows $4 \times 4 \times 4$ which can be written as $\qquad$ and is said '4 $\qquad$ '.
Diagram B shows $3 \times 3 \times 3 \times 3$ or $\qquad$ .

1. Write the following calculations using index notation:
a) $6 \times 6$
b) $6 \times 6 \times 6 \times 6$
c) $2 \times 2 \times 2 \times 2 \times 2$
2. Find the product of Q 1 parts a) and b), write the answer in index notation.
3. Copy the equations below. Circle those that are true, and cross through those that aren't true.

$$
9^{1}=9 \quad 5^{3}=25 \times 5
$$

$$
5^{3}=3 \times 3 \times 3 \times 3 \times 3 \quad 10^{2}=2^{10}
$$

$$
8^{3}=24
$$

$$
8^{4}=8 \times 8 \times 8 \times 8
$$

4. Place the correct symbol (<, >, or $=$ ) between each pair of numbers
a) $2^{3}$ $\qquad$ $3^{2}$
b) $2^{4}$ $\qquad$ $4^{2}$
c) $3^{3}$ $\qquad$ $5^{2}$
d) $1^{8}$ $\qquad$ $1^{5}$
5. Organise the diagrams into the following groups:

6. Match the calculations on the left to the versions written in index form.
$2 \times 2 \times 7 \times 7 \times 7$
$5^{3} \times 3$
$5 \times 3 \times 5 \times 3$
$2^{2} \times 3^{2} \times 5^{2} \times 7$
$7 \times 7 \times 5 \times 5 \times 3 \times 3 \times 5 \times 7$
$3^{2} \times 5^{2}$
$5 \times 5 \times 3 \times 3 \times 2 \times 2 \times 7$
$2^{2} \times 7^{3}$
$5 \times 5 \times 5 \times 3$
$3^{2} \times 5^{3} \times 7^{3}$
7. $3^{a}>100$. Find the smallest integer value of $a$.
8. $2^{b}$ is a square number. Find three different possible values for $b$.

## Questions for depth:

1. Use the associative property of multiplication to write these calculations using index notation
a) $2 \times 4$
b) $5 \times 15$
c) $3 \times 12$

## Week 3 Session 2: Prime factors

Concept Corner



Prime numbers, like 5 and $\qquad$ can be multiplied together to make other numbers.


For example, 2 s and 3 s can be multiplied to make $\qquad$ .

Prime numbers $\qquad$ be made by multiplying smaller primes.

All non-prime numbers greater than 2 can be made by multiplying $\qquad$ numbers, e.g. $70=2 \times$ $\qquad$ $\times 7$.

1. Copy and complete the frames to find ways of showing the numbers as products of different combinations of factors.
a) $24=\ldots \times \ldots$
b) $120=\ldots \times \ldots$
$\qquad$ $120=$ $\qquad$ $\times$ $\qquad$
$\qquad$
$24=$ $\qquad$
$\qquad$ $\times$ $\qquad$
$120=$ $\qquad$ $\times \ldots \times$ $\qquad$ $\times$
2. Copy and complete so that each equation shows a number as the product of prime factors.
a) $12=2 \times 3 \times \ldots$
b) $20=\ldots \times 2 \times 5$
c) $30=2 \times \ldots \times 5$
d) $36=\ldots \times 2 \times 3 \times 3$
e) $45=3 \times$ $\qquad$ $\times$
f) $54=2 \times 3 \times$ $\qquad$ $\times$
3. Rewrite the following products so that only prime factors are used
a) $24=2 \times 3 \times 4$
b) $48=2 \times 24$
c) $60=4 \times 15$
d) $72=4 \times 2 \times 9$
4. How many different products can you find by placing different combinations of the factor cards into the frame?

5. Gavin and Brenda have chosen a list of factors to multiply together.

Gavin has shaded in the numbers he thinks he can make by multiplying these factors (he can use factors more than once in each multiplication).

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 |
| 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 |
| 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 |
| 51 | 52 | 53 | 54 | 55 | 56 | 57 | 58 | 59 | 60 |
| 61 | 62 | 63 | 64 | 65 | 66 | 67 | 68 | 69 | 70 |
| 71 | 72 | 73 | 74 | 75 | 76 | 77 | 78 | 79 | 80 |
| 81 | 82 | 83 | 84 | 85 | 86 | 87 | 88 | 89 | 90 |
| 91 | 92 | 93 | 94 | 95 | 96 | 97 | 98 | 99 | 100 |


a) Show how Gavin can make the following numbers by multiplying factors from his list:
i) $28=$
ii) $63=$
iii) $42=$
b) Do you agree that Brenda will be able to make all multiples of 11? Explain why or why not.
c) Gavin thinks he could remove factors from the list and still make all the shaded numbers.

Which factors could he remove? Why?

## Questions for depth:

The grid has been shaded in the same way as in question 4) above, using a list of seven factors.

1. What was the list of factors?
2. What are the next three numbers greater than 100 that can be shaded?

| 1 | 2 | 3 | 4 | 5 | 6 | 7 | 8 | 9 | 10 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 11 | 12 | 13 | 14 | 15 | 16 | 17 | 18 | 19 | 20 |
| 21 | 22 | 23 | 24 | 25 | 26 | 27 | 28 | 29 | 30 |
| 31 | 32 | 33 | 34 | 35 | 36 | 37 | 38 | 39 | 40 |
| 41 | 42 | 43 | 44 | 45 | 46 | 47 | 48 | 49 | 50 |
| 51 | 52 | 53 | 54 | 55 | 56 | 57 | 58 | 59 | 60 |
| 61 | 62 | 63 | 64 | 65 | 66 | 67 | 68 | 69 | 70 |
| 71 | 72 | 73 | 74 | 75 | 76 | 77 | 78 | 79 | 80 |
| 81 | 82 | 83 | 84 | 85 | 86 | 87 | 88 | 89 | 90 |
| 91 | 92 | 93 | 94 | 95 | 96 | 97 | 98 | 99 | 100 |

## Week 3 Session 3: Prime factorisation

Concept Corner


Numbers such as 18 and 45 are called $\qquad$ integers and can be built as the
$\qquad$ of prime factors.
e.g. 45 can be written as $\qquad$ $\times 3 \times 5$, or $3^{2} \times 5$ in $\qquad$ notation.

1. Copy and complete the prime factorisation trees and write the numbers as products of prime factors.
a)

b)

$90=$ $\qquad$

$$
36=
$$

$\qquad$
c)

$42=$ $\qquad$
d)

2. Write the following numbers as products of their prime factors.:
a) 72
b) 175
c) 144
d) 1750
e) 350
f) 216
3. Brenda is writing out the prime factor tree for 84 . Gavin is commenting on her working.


You've started incorrectly. Neither 4 nor 21 are prime.


Who do you agree with? Explain your answer. You may use examples to help.
4. Look at your answers to question 2. and answer the questions below.
a) Compare the prime factors of parts a), c) and f). What do you notice?
b) Compare the prime factors of parts b), d) and e). What do you notice?
c) Write down the prime factors of 720. Explain how you can use your answer to 2a) to help.
5. The cards below show three different numbers $\boldsymbol{a}, \boldsymbol{b}, \boldsymbol{c}$ and $\boldsymbol{d}$ written as products of their prime factors.
Decide if the statements below are true or false.

$$
\begin{array}{ll}
a=2 \times 3^{2} \times 5^{2} \\
c=2^{3} \times 3^{2} \times 5^{3} & b=2 \times 3^{2} \times 5^{3} \\
d=2^{2} \times 3^{2} \times 5^{2}
\end{array}
$$

a) $\boldsymbol{d}$ is twice the value of $\boldsymbol{a}$
b) $\boldsymbol{c}$ is three times the value of $\boldsymbol{b}$
c) $\boldsymbol{c}$ is ten times the value of $\boldsymbol{d}$
d) $\boldsymbol{b}$ is less than $\boldsymbol{d}$

## Questions for depth:

1. Two numbers, $m$ and $n$ have been written as the products of their primes, where $\mathrm{x}, \mathrm{y}$ and z are different prime numbers. Decide whether the statements below are true or false.
a) $\boldsymbol{m}$ and $\boldsymbol{n}$ can be equal in value

$$
m=x^{2} \times y^{3} \times z^{4}
$$

b) $\boldsymbol{m}$ and $\boldsymbol{n}$ are square numbers
c) $\boldsymbol{m}$ and $\boldsymbol{n}$ are multiples of $\left(x^{2} \times y^{2} \times z^{2}\right)$

## Week 3 Session 4: Using the prime factorisation

## Concept Corner

Prime factorisations can be used to deduce factors of a number:

$$
84=2^{2} \times 3 \times 7=12 \times 7
$$



In the example above the $\qquad$ factors 2,2 , and 3 have been multiplied together showing us that $\qquad$ and $\qquad$ are a factor $\qquad$ of 84 .

Using a similar approach another factor pair of 84 can be made:
$2 \times 2=$ $\qquad$ $3 \times 7=21$

So, 4 and $\qquad$ are a factor pair of 84 .

1. Copy and complete the prime factorisation trees and write the numbers as products of prime factors.
a)

b)

$30=$ $\qquad$
c)


$$
20=
$$

$\qquad$
$42=$
$\qquad$
d)

$70=$ $\qquad$
2.
a) Use your answers to question 1 to help work out how many factors each of the numbers 30, 42, 20 and 70 has.
b) What's the same or different about the number of factors each number has? Explain why this is the case.
c) Find a number that has the same number of factors
3. The numbers in the box below have been written as the product of their prime factors. Use this information to help you answer the questions below.

$$
\begin{array}{cc}
72=2^{3} \times 3^{2} & 75=3 \times 5^{2} \\
168=2^{3} \times 3 \times 7 & \mathbf{3 0}=2 \times 3 \times 5 \\
245=5 \times 7^{2} & \mathbf{4 2}=2 \times 3 \times 7
\end{array}
$$

a) $75=15 \times$ $\qquad$
c) Two of the numbers multiply to make a square number, which two?
b) Does 168 have a factor that is a square number?
d) The product of all of the numbers in the box is 280052640000 . Write 280052640000 as a product of prime factors
4. $2 \times 3^{3} \times 5=270$

Every factor pair for 270 will have one even factor and one odd factor.

Do you agree or disagree with Nicola? Explain why.

5. $210=2 \times 3 \times 5 \times 7 \quad 220=2^{2} \times 5 \times 11 \quad 230=2 \times 5 \times 23$

Which of these numbers has the most factors? Which of these numbers has the least factors?
6. Which of the numbers below has the greatest factor?
$315=3^{2} \times 5 \times 7$
$210=2 \times 3 \times 5 \times 7$
$220=2^{2} \times 5 \times 11$

## Questions for depth:

1. Look at the number below written as the product of its prime factors.

$$
42336=2^{5} \times 3^{3} \times 7^{2}
$$

a) $42336 \div a$ results in an odd integer. What are the greatest and least possible values of $a$ ?
b) $42336 \times b$ results in a cube number. What are the greatest and least possible values of $b$ ?

## Week 4: Prime factorisation 2

## Session 1: Highest common factor

## Concept Corner




The highest common factor, abbreviated as the $\qquad$ can be found by listing the
$\qquad$ of each number.

We can use the diagram to see that the HCF of 30 and 45 is $\qquad$ .

1. List all of the factors of:
a) 28
b) 54
c) 36
d) 19
2. Identify all the common factors of:
a) 28 and 54
b) 28 and 36
c) 28 and 19
d) 54 and 36
3. Find the HCF for the pairs in Q2.
a) What size squares has this student split the rectangle in to?
b) What other squares size squares can you split it into?

4. 

a) Find three pairs of numbers that have a HCF of 12 .
b) What other factors do the pairs have in common?
5. Find the HCF of the following:
a) 12 and 18
b) 12 and 30
c) 12 and 42
d) 12 and 54
e) 16 and 24
f) 40 and 24
g) 64 and 24
h) 88 and 24
6. A shop sells boxes of chocolate. In total there are 252 dark chocolates and 180 milk chocolates. If every box is identical, how many boxes could there be?

7. A pair of distinct two-digit numbers have a common factor of 16 .
a) Find three possible pairs
b) Find all the possible values for the HCF.

## Questions for depth:

1. How else can you split the cuboid into identical cubes? Explore this for different sized cuboids.


## Week 4 Session 2: More highest common factor

## Concept Corner



$$
\begin{aligned}
& 60=2 \times 2 \times 3 \times 5 \\
& 84=2 \times 2 \times 3 \times 7
\end{aligned}
$$



Writing numbers as a $\qquad$ of their $\qquad$ factors helps to reveal common factors. The Venn diagram shows the prime factors of $\qquad$ and $\qquad$ We can see that $\qquad$ is a common factor and $\qquad$ is the $\qquad$ _.

1. Write each of the numbers as a product of primes:
a) 130
b) 104
c) 56
d) 308
2. Given that $1680=2 \times 2 \times 2 \times 2 \times 3 \times 5 \times 7$
a) Decide whether each of the following are factors of 1680:
i. 2
ii. 7
iii. 14
iv. 13
v. 8
vi. 11
vii. 32
viii. 48
b) Which of the numbers from Q1 is a factor of 1680 ?
3. Copy and complete the Venn diagrams:
a)

b)

c)

d)

4. Find the highest common factor of each pair
a) 130 and 104
b) 130 and 308
c) 56 and 104
d) 56 and 308
e) 130 and 56
f) 308 and 104
5. Place the primes into the Venn diagram. Find the possible pairs of numbers and their highest common factors:

6. Find three examples of a pair of numbers greater than 1000 that have a HCF of 72.
7. A rectangular field needs to be divided in to equally sized, square plots of land. How large can the squares be?


## Questions for depth:

1. Compare the HCF of $\boldsymbol{a}$ and $\boldsymbol{b}$ with the HCF of $\boldsymbol{a}$ and $\boldsymbol{a}+\boldsymbol{b}$. Select your own values for $a$ and $b$. What do you notice? Will this always be true? Explain your answer.

## Week 4 Lesson 3: Lowest common multiple

Concept Corner


Multiples of 3:
$3,6,9$, 12 $, 15,18,21$, (24), 27,30
Multiples of 4: 4,8 , (12) 16,20 , (24, $28,32 \ldots$


The $\qquad$ common multiple, abbreviated as the $\qquad$ can be found by listing the $\qquad$ of each number.

We can see that the LCM of 3 and 4 is $\qquad$ .

1. List the first 12 multiples of:
a) 12
b) 9
c) 7
d) 21
2. Identify the lowest common multiple of:
a) 12 and 9
b) 12 and 7
c) 12 and 21
d) 21 and 7
e) 21 and 9
f) 9 and 7
3. Find three examples of a pair of numbers that have a LCM of
a) 15
b) 21
c) 30
d) 36
4. A cicada lives underground and appears every 17 years. A predator of the cicada appears every 4 years. If they hide at the same time, how long will it be before they appear again at the same time?

5. Charlie is trying to create a squares by tessellating the rectangle below. What size squares can he make?

6. Select two side lengths from the numbers below. Explore the different squares you can make by tessellating the rectangle:

7. A takes 12 seconds to do a full turn, B takes 21 seconds. They repeatedly spin in the same direction starting in the position shown:

a) How much time passes before $A$ and $B$ return to their starting position at the same time?
b) Will your answer change if they spin in opposite directions? If so, how?

## Questions for depth:

1. Following on from the situation in Q7:
a) When is the first time that the arrows point in the same direction?
b) Can the arrows both point upwards at the same ti

## Week 4 Session 4: More lowest common multiple

## Concept Corner



$$
\begin{aligned}
& 60=2 \times 2 \times 3 \times 5 \\
& 84=2 \times 2 \times 3 \times 7
\end{aligned}
$$



Writing numbers as a $\qquad$ of their $\qquad$ factors helps you to find the lowest common multiple.

The Venn diagram shows the prime factors of 60 and 84 . We can see that the $\qquad$ is $\qquad$ $\times 7=$ $\qquad$ $\times 5=$ $\qquad$

1. Write each of the numbers as a product of primes:
a) 63
b) 84
c) 52
d) 36
2. Copy and complete the Venn diagrams:
a)

b)

c)

d)

3. Find the lowest common multiple of each pair:
a) 84 and 63
b) 84 and 52
c) 36 and 63
d) 36 and 52
e) 84 and 36
f) 63 and 52
4. Place the primes into the Venn diagram. Find the possible pairs of numbers and their lowest common multiples:

5. Find examples of pairs of two digit numbers with a LCM greater than 1000.

## Questions for depth:

1. Find the product of the highest common factor and the lowest common multiple for different pairs of numbers. What do you notice? Why does this happen?
2. Neda is investigating the number of squares that a rectangle's diagonal crosses. Investigate how many squares are crossed for different rectangles. What do you notice?


## Week 5: Fractions

## Session 1: Part of a whole

## Concept Corner

We can use fraction notation to describe part of a $\qquad$ _.

The $\qquad$ represents the total number of equal parts, the $\qquad$ represents the number of parts we are describing.

E.g. if $\square$ is the whole.

The shaded section of $\square$ represents $\qquad$ or " $\qquad$ ".

The unshaded section of $\square$ represents $\qquad$ or " $\qquad$ ".

1. Find the matching pairs
a) $\frac{2}{3}$
b) $\frac{2}{5}$
c) $\frac{4}{3}$
d) $\frac{3}{2}$
e) $\frac{3}{4}$

Four thirds


Three quarters
2. a) Write the values of the marked points of the number line:
i) $\quad \mathrm{A}=$
ii) $\mathrm{B}=$
iii) $\mathrm{C}=$

b) Suggest a value in fraction notation that lies between:
i) 0 and A : $\qquad$
ii) A and B: $\qquad$ iii) 1 and C: $\qquad$
3. If
 1, write a fraction to represent the value of the shaded section:
a)

b)

c)

4. Draw a copy of the numberline and identify where the shapes should be placed:



A


B


C


D
5. Sketch a diagram to complete the statement:
e.g.

is $\frac{1}{4}$ of

a)

is $\frac{1}{2}$ of $\qquad$
b)

is $\frac{1}{3}$ of $\qquad$
c)

is $\frac{2}{3}$ of
$\qquad$
d)

f)

$\qquad$

## Questions for depth:

1. Tom thinks that that you will always be able to find a fraction 'in between' two other fractions. Do you agree with him? Why?
e.g.


## Week 5 Session 2: Fractions of measure

Concept Corner
We can use $\qquad$ when describing units of measure.

Units of measure can be used to describe: $\qquad$ , $\qquad$ , angles, volume etc.


For example if a cube holds 1 L of water
1 L

Here
we have $\qquad$ of water.

1. Each of the following shapes has an area of $1 \mathrm{~m}^{2}$
a) Find the area of:

i)

ii)

iii)

iv)

$\qquad$
2. A cube can hold 1 L of water:
.How much water is shown below?
3. This clock shows 06:00.
a) How many minutes will have past when the minutes hand has travelled $\frac{1}{4}$ of the way around the clock?
b) What fraction of the clock will the hour hand have travelled by 10:00?

c) What fraction of the clock will the hour hand have travelled when the minute hand has travelled all the way around the clock?
d) What fraction of the clock will the hour hand have travelled when the minute hand has travelled half way around the clock?
4. If each flag has an area of $1 \mathrm{~m}^{2}$, find the areas of each colour in fraction notation:
a)
b)
c)


5. Sketch three flags where $\frac{1}{4}$ of the area is white,$\frac{1}{4}$ is black and $\frac{1}{2}$ is grey.

## Questions for depth:

1. A 1 m length of rope is made into a circle. Find the length of each section of rope:


## Week 5 Session 3: Fair shares

## Concept Corner

We can use $\qquad$ notation to describe a $\qquad$


1. State the value of the shaded and unshaded sections:

a)

b)

c)

d)


e) $\square$

2. Find the missing numbers below:
a)

b)

3. Write the following questions in fraction notation
a) $2 \div 3$
b) $3 \div 4$
c) 5 divided by 3
4. A group of friends are sharing 2 chocolate bars. What fraction of a chocolate bar do they each get if ..

a) ... there are 3 friends?
b) ... there are 5 friends?

Sketch diagrams to represent each situation
c) ... there are 7 friends?
5. In each situation decide which group gets more soda per person.

How much do they get each?
a)

b)

c)


6. A group of 7 people plan to share 4 L of soda. Two people join the party and bring 1 L of soda. Does the amount of soda per person increase or decrease?


## Questions for depth:

1. n people plan to share 10 chocolate bars.
a) How much does each person get?

2 more people join the group and bring a chocolate bar with them...
b) When does the amount of chocolate per person increase? When does it decrease?

## Week 5 Session 4: Equivalence

Concept Corner
Two fractions are said to be $\qquad$ if they represent the same value.

For example we can see that $\qquad$ $=$ $\qquad$ so they are equivalent. Similarly, $\qquad$ $=$ $\qquad$ so they are equivalent too.

| $\frac{1}{3}$ |  | $\frac{1}{3}$ |  | $\frac{1}{3}$ |  |
| :---: | :---: | :---: | :---: | :---: | :---: |
| $\frac{1}{6}$ | $\frac{1}{6}$ | $\frac{1}{6}$ | $\frac{1}{6}$ | $\frac{1}{6}$ | $\frac{1}{6}$ |

1. What fraction of a hexagon is shaded?
a)


b)

c)

d)

e)

e)

6
$\frac{1}{1}$

$\frac{-\cdots}{6}$


2. 

a) Find each of the marked decimal values on this tape measure:

b) Now write each of the answers in the form: $\frac{\square}{10}$
3.
a) Find the marked numbers:

b) Use the number lines to find different ways to complete the following:

$$
\frac{\cdots}{3}=\frac{3}{6}
$$

4. Here are three fractions that are equivalent to $\frac{3}{4}$ :
$\frac{3}{4}$

Draw your own diagrams to show three fractions equivalent to:
a) $\frac{2}{3}$
b) $\frac{4}{5}$
c) $\frac{4}{3}$
5. Copy and complete each of the following:
a) $\frac{1}{2}=\frac{\square}{10}=\square$
b) $\frac{1}{5}=\frac{\square}{10}=\square \cdot \square$
c) $\frac{2}{5}=\frac{\square}{10}=\square$
d) $\frac{\square}{5}=\frac{12}{10}=\square$
е) $\frac{\square}{\square}=0.7$
f) $\frac{12}{30}=\frac{\square}{10}=\square$
g) $\frac{36}{20}=\frac{\square}{10}=$
h) $\frac{8}{25}=\frac{\square}{100}=\square$
i) $\frac{\square}{50}=\frac{\square}{100}=06$
6. Charlie has shown how he would share two sausages between three people.
a) What fraction of a sausage does each person get?
b) Draw a similar diagram to show the following. What fraction of a sausage does each person get?

i) 4 sausages between 6 people
ii) 4 sausages between 3 people
iii) 8 sausages between 6 people

## Questions for depth:

1. 

a) What fraction of the crocodile's total length is its:
i) head?
ii) body?
iii) tail?
b) The world's longest recorded crocodile, Lolong, was 6.17 m long! Assuming it had the same proportions, find the approximate length of its head, body and tail.


## Week 6: Fractions 2

## Session 1: Comparing fractions

## Concept Corner

We can use our understanding of the $\qquad$ and denominator to $\qquad$ fractions. This diagram shows that $\frac{1}{8}-\frac{1}{12}$.


We can also use this to compare fractions as a distance from another point. For example, $\frac{11}{12}>\frac{7}{8}$ since $\frac{11}{12}$ is closer to 1 . We can also see that $\frac{7}{12}-\frac{5}{8}$ when we compare their distances from $\frac{1}{2}$.


1. Decide which fraction is greater, copy and complete the inequality with < or >.
a) $\frac{1}{3} \frac{2}{3}$

b) $\frac{3}{5} \frac{2}{5}$

c) $\frac{1}{2} \frac{3}{2}$

2. Use the diagram to find three equivalent fractions:
a)

b)



$$
\frac{a}{\square}=\frac{\square}{\square}
$$

$$
\frac{\square}{\square}=\frac{a}{\square}=\frac{\square}{\square}
$$

$$
\frac{\square}{\square}=\frac{\square}{\square}
$$

a) Copy and complete the following:

$$
\frac{1}{2}=\frac{\square}{6} \text { and } \frac{2}{3}=\frac{\square}{6} \text { so } \frac{1}{2} \square \frac{2}{3} \square \square \square
$$

b) Compare $\frac{2}{3}$ and $\frac{3}{5}$ using a similar strategy
3. Copy and complete each inequality with < or > :
a) $\frac{1}{5}: \frac{2}{15}$
c) $\frac{3}{4}: \frac{11}{16}$
b) $\frac{3}{7}$
d) $-\frac{1}{2}$
4. Which of these fractions is:
a) Closest to 1
b) Closest to $\frac{1}{2}$

c) Largest
5.
a) Fill in the blanks
i) $\frac{3}{}=\frac{1}{2}$
ii) $\frac{2}{3}=\frac{6}{\square}$
iii) $\frac{5}{\hdashline-\ldots}<\frac{1}{2}$
iv) $\frac{2}{3}>\frac{-}{18}$
b) Find a value that satisfies both of the inequalities for part a iii) and iv)

## Questions for depth:

1. How many ways can you complete the following inequality?

$$
\frac{3}{4}<\frac{}{16}<\frac{7}{8}
$$

Design your own inequality problem using the following template:

$$
\frac{a}{\square-\cdots}<\frac{\square}{-\cdots}
$$

## Week 6 Session 2: Common denominators

## Concept Corner

We can systematically compare two fractions by finding a $\qquad$ denominator.

This also helps us to accurately describe the $\qquad$ between fractions.
e.g. $\frac{2}{5}$ is $\frac{1}{15}$ $\qquad$ than $\frac{1}{3}$


1. Use these diagrams to calculate equivalent fractions for $\frac{2}{5}$
a)

b)

c)


2. a) Shade in the diagrams to show
i) $\frac{2}{3}$

ii) $\frac{3}{4}$

iii) $\frac{1}{2}$

iv) $\frac{5}{6}$

b) Write each of the fractions in part a) as $\frac{\text { and }}{12}$
c) Write each of the fractions in part a) in order from smallest to greatest.
3. a) Fill in the blanks:
i) $\frac{1}{4}=\frac{6}{\square}$
ii) $\quad \frac{1}{5}=\frac{6}{\square}$
iii) $\quad \frac{2}{3}=\frac{6}{\square}$
iv) $\quad \frac{3}{13}=\frac{6}{\square}$
b) Write each of the fractions in part a) in order from smallest to greatest
4. 



This diagram shows $\frac{17}{30}$. Use the diagrams to work out how much greater each fraction is than $\frac{17}{30}$.

a)

$\frac{3}{5}$
b) $\frac{5}{6}$
c) $\frac{2}{3}$

5. Use a similar method to decide which of the fractions is greater, and how much greater:
a) $\frac{4}{5}$ or $\frac{5}{7}$
b) $\frac{5}{6}$ or $\frac{9}{11}$
c) $\frac{3}{10}$ or $\frac{4}{15}$
d) $\frac{9}{8}$ or $\frac{23}{20}$
6. 3 friends share a chocolate bar. Polly ate $\frac{2}{5}$ of the chocolate bar, Kim ate $\frac{3}{7}$ of the chocolate bar, and Niels ate the rest.
a) Who ate more, Polly or Kim?

b) What fraction did Niels eat?

## Questions for depth:

1. 

a) How many ways can you use the integers $1-6$ to complete the following:

b) In which solution(s) is the smallest and largest fra

## Week 6 Session 3: Decimal fractions

## Concept Corner

We can use $\qquad$ notation to help us order fractions.

For example from the diagram we can see that $\qquad$ $>$ $\qquad$


Writing fractions in decimal notation can help us to order. e.g. $\frac{9}{10}=$ $\qquad$ and $\frac{21}{25}=$ $\qquad$ so $\frac{9}{10}>\frac{21}{25}$

1. For each diagram decide what decimal is represented by:
i) the shaded section
ii) the white section
a)
b)

c)

d)

iii) Place the four decimal fractions in ascending order.
2. Copy and complete the equivalent statements for:
i) the shaded section
ii) the white section
a)

b)


$$
\frac{\square}{5}=\frac{\square}{10}=
$$

$\frac{\square}{4}=\frac{\square}{100}=$
3.
a) Copy and complete the following:

$$
\begin{gathered}
\frac{3}{10}=\frac{31}{100}=\frac{2}{5}=\frac{\square}{10}=\square \\
\frac{17}{50}=\frac{\square}{100}=\square
\end{gathered}
$$

b) Write the fractions in ascending order
c) Find a fraction that lies between $\frac{31}{100}$ and $\frac{8}{25}$, write it in decimal form.
4. How many numbers can you create by placing the number cards, without repeats, in to the spaces? Record them in ascending order.

5. How many different fractions can you create by selecting two of the cards to be the numerator and denominator of the fraction?

Write each fraction in decimal notation and record them in ascending order.

## Questions for depth:



1. How many was can you complete the following, with no repeats?


## Week 6 Session 4: Mixed comparisons

## Concept Corner

Depending on the situation, different $\qquad$
for $\qquad$ fractions can be more or less useful.

For example you could deduce that:
$\frac{1}{3}-\frac{1}{5} \quad$ by comparing their $\qquad$ .
$\frac{17}{50}-0.32 \quad$ by noting that $\frac{17}{50}=$ $\qquad$


1. What decimals are shown on the numberline?

2. Find the size of the interval in each of the number lines:

> For example...

a)

b)

c)

d)

e)

f)

g)

h)

i)

3. Draw your own numberline, with an appropriate scale, indicating:

$$
0.3,0.7,-1.5 \text { and 2.3. }
$$

4. Copy and complete the following, use the correct symbol $>,<$ or $=$.
а) $\frac{3}{4}: \frac{1}{4}$
b) $\frac{1}{5}: \ldots \frac{1}{4}$
c)


d)

e)
0.6

f)

g) 0.25

h) 0.23

i) $\quad 0.3$

5. Copy and complete the numberline:

6. How many was can you insert two of the cards in to the spaces to make the statements true:

a) $\frac{1}{\square}<\frac{1}{\square}$
b) $0 .<\frac{1}{\square}$
c) $\frac{1}{\square}<0$.


## Questions for depth:

1. Charlie thinks that you can find a fraction that lies in between any pair of numbers. Do you agree? Explain your reasoning.

## Week 7: Fractions 3

## Session 1: Modelling multiplication I

## Concept Corner

When $\qquad$ fractions and integers, it is useful to use models to investigate the calculation.

If we want to multiply 3 and $\frac{1}{4}$
 we can consider 3 $\qquad$
$\frac{1}{4}$. Alternatively, we can consider $\frac{1}{4}$ of 3 . We know this will give the same answer because of the $\qquad$ property of multiplication.

1. What unit fraction is represented?
a)


e.g. $\frac{1}{2}$

$\qquad$


b)

c)

2. Tom drew a diagram that represents: $6 \times \frac{1}{2}=3$
a) Draw your own diagram to represent:
i) $6 \times \frac{1}{3}$
ii) $8 \times \frac{1}{4}$
iii) $3 \times \frac{1}{4}$
iv) $4 \times \frac{1}{3}$
b) Work out the value of each calculation.
c) Write a word problem for each of the calculations
3. Andi drew a different model to represent $\frac{1}{2} \times 6=3$
a) Draw a similar diagram to represent:

i) $\frac{1}{3} \times 12$
ii) $\frac{1}{5} \times 35$
iii) $\frac{1}{2} \times 3$
iv) $\frac{1}{4} \times-20$
b) Work out the value of each calculation.
4. Copy and complete the calculations:
a) $\frac{1}{3} \times 12=12 \times \ldots=$
b) $\frac{1}{3} \times$ $\qquad$ $=\ldots \times$ $\times \frac{1}{3}=8$
c) $\frac{1}{6} \times 12=12 \times \ldots=$
d) $\frac{1}{6} \times \ldots=\ldots \times \frac{1}{6}=4$
e) $\frac{1}{6} \times 18=\ldots \div-\ldots$
f) $7 \times \frac{1}{5}=$ $\qquad$ $\div 5=$ ?
g) $\frac{1}{7} \times n=\ldots \div 7=$ $\qquad$
h) $n \times \frac{1}{m}=$ $\qquad$ $\div-$ $=\frac{?}{?}$
5. Write a word problem for each calculation in Q5.
6. Find ten pairs of numbers whose product is 1 .

## Questions for depth:

1. Plot each of the pairs in Q 7 as a coordinate on an $x$ and $y$ axis.
e.g. $\quad \frac{1}{2} \times 2=1$ plot the pair $\left(\frac{1}{2}, 2\right)$
2. 

a) Find the value of: $\left(\frac{1}{6} \times 5\right) \times\left(8 \times \frac{1}{5}\right) \times\left(6 \times \frac{1}{8}\right)$
b) Find similar products that have the same value.

## Week 7 Session 2: Modelling multiplication II

## Concept Corner

We can apply the same models to multiplying non-unit fractions. In this example, the
$\qquad$ of $\frac{2}{3}$ and 6 can be found by working out 6 lots of $\frac{2}{3}$, or by working out $\frac{2}{3}$ of $\qquad$ .

These models also apply to percentages, e.g. $30 \% \times 40=\frac{30}{100}$ of $40=40$ lots of $\frac{30}{100}$

1. What number is represented? Write your answer as a fraction, decimal and percentage.
a)

b)

c)

2. Tom drew a diagram that represents: $8 \times \frac{3}{4}=6$
a) Draw your own diagram to represent:

i)
$3 \times \frac{2}{3}$
ii) $4 \times \frac{3}{4}$
iii) $9 \times \frac{2}{3} \quad$ iv) $5 \times \frac{2}{3}$
b) Work out the value of each calculation.
c) Write a
tion.
3. Copy and complete the following:
a) $\frac{1}{4} \times 12=12 \div-$
b) $\frac{3}{4} \times 12=12 \div-\ldots=$ $\qquad$ c) $\frac{5}{4} \times 12=12 \div \ldots \times=$
d) $2 \times \frac{1}{5}=2 \div-=$
e) $2 \times \frac{4}{5}=$ $\qquad$ $\div-$ $\times 4=$ $\qquad$ f) $2 \times \frac{7}{5}=$ $\qquad$
4. Write each of the calculations in Q3 as decimal multiplications.

$$
\text { e.g. } \frac{1}{4} \times 12=0.25 \times 12
$$

5. Copy and complete the following:
a) $0.3=\frac{?}{10}=\frac{?}{100}$
b) $0.25=\frac{?}{4}=\frac{?}{100}$
c) $0.75=\frac{?}{4}=\frac{?}{100}$
d) $0.3 \times 70=$ $\qquad$ e) $44 \times 0.25=$
f) $0.75 \times 28$
g) $30 \%$ of 12
h) $25 \%$ of 44
i) $75 \%$ of 28
6. Draw enlarged versions of the shapes below by a scale factor of:
a) 0.6
b) $\frac{2}{5}$
c) 0.8


Questions for depth:

1. A monkey starts with 75 bananas.

- He eats $\frac{1}{3}$ of them and throws one away.
- He then eats $\frac{4}{7}$ of what is left and throws one away.
- He then eats $\frac{9}{10}$ of what is left and throws one away.
a) How many does he have left over?
b) How can you change the three fractions and e


## Week 7 Session 3: Multiplying fractions I

## Concept Corner

We can use an $\qquad$ to help us multiply two fractions. This diagram shows a that the product of $\frac{2}{3}$ and $\frac{4}{5}$ is $\qquad$ -.

The $\qquad$ is represented by the shaded
area, and is a rectangle with an $2 \times 4$ parts.
The $\qquad$ is represented by entire square, and is divided into $3 \times 5$ parts.

This can be thought of as " 2 thirds of 4 fifths" or
" 4 fifths of 2 thirds".


1. Use the diagram to copy and complete the calculations:

$\frac{1}{2}$ of $\frac{1}{2}$ is $\qquad$ $\frac{1}{2} \times \frac{1}{2}=$ $\qquad$
b)


$$
\frac{1}{2} \text { of } \frac{1}{3} \text { is } \quad \frac{1}{2} \times \frac{1}{3}=
$$

$\qquad$

$\frac{1}{3}$ of $\frac{1}{2}$ is $\qquad$ $\frac{1}{3} \times \frac{1}{2}=$ $\qquad$ $\frac{1}{3}$ of $\frac{1}{3}$ is $\frac{1}{3} \times \frac{1}{3}=$ $\qquad$

$\frac{1}{4}$ of $\frac{1}{2}$ is $\qquad$ $\frac{1}{4} \times \frac{1}{2}=$ $\qquad$ $\frac{1}{4}$ of $\frac{1}{3}$ is $\quad \frac{1}{4} \times \frac{1}{3}=$ $\qquad$
2. Draw your own diagrams, to illustrate the following calculations:
a) $\frac{1}{2} \times \frac{1}{5}$
b) $\frac{1}{3} \times \frac{1}{5}$
c) $\frac{1}{4} \times \frac{1}{5}$
d) $\frac{1}{5} \times \frac{1}{2}=$
e) $\frac{1}{5} \times \frac{1}{3}$
$1 \quad 1$
3. Use the diagrams to copy and complete the calculations:
 $\frac{2}{3}$ of $\frac{2}{3}$ is $\quad \frac{2}{3} \times \frac{2}{3}=$ $\qquad$
4. Calculate the following, simplify your answers:
a) $\frac{1}{3} \times \frac{1}{5}$
b) $\frac{2}{3} \times \frac{1}{5}$
c) $\frac{3}{3} \times \frac{1}{5}$
d) $\frac{2}{3} \times \frac{4}{5}$
e) $\frac{2}{3} \times \frac{5}{5}$
f) $\frac{2}{3} \times \frac{6}{5}$
5. Find five pairs of fractions whose product is ...
a) $\frac{1}{2}$
b) 1
c) $\frac{7 \times 5}{6 \times 8}$
6. Copy and the complete the following:
a) $\frac{3}{5} \times \frac{5}{7}=\frac{\square \times}{5 \times 7}=\frac{\square}{5} \times \frac{3}{7}=\square \times \frac{3}{7}=\frac{\square}{\square}$
b) $\quad \frac{3}{5} \times \frac{10}{7}=\frac{\square \times \square}{5 \times 7}=\frac{\square}{5} \times \frac{3}{7}=\frac{\square}{7}=\frac{\square}{\square}$

## Questions for depth:

1. Place the following in ascending order:
a) $\left(\frac{2}{3}\right)^{2}$
b) $\left(\frac{2}{3}\right)^{3}$
c) $\frac{2}{3} \times \frac{4}{5}$
d) $\left(\frac{2}{3}\right)^{2} \times \frac{4}{5}$
e) $\left(\frac{4}{5}\right)^{3}$
2. Does squaring a number increase its value? Explain

## Week 7 Session 4: Multiplying fractions II

## Concept Corner

By converting $\qquad$ to
fractions, we can use the same model to find the product of decimals.
E.g.

$0.7 \times 0.3=\frac{7}{7} \times \frac{7 \times 3}{10 \times 10}=\frac{1}{100}=0.21$

1. What number is represented? Write your answer as a fraction and a decimal.
a)



b)

2. Copy and complete the following:
a) $0.4 \times 0.6=\frac{\square}{10} \times \frac{\square}{10}=\frac{\square}{100}=\square . \square$
b) $0.2 \times 0.9=\frac{\square}{10} \times \frac{\square}{10}=\frac{\square}{100}=\square$
c) $0.2 \times 1.5=\frac{\square}{5} \times \frac{\square}{2}=\frac{\square}{10}=\square$
d) $1.2 \times 1.5=\frac{\square}{5} \times \frac{\square}{2}=\frac{\square}{10}=\square$
3. Draw a model to illustrate two of the calculations in Q2. For example:

4. Copy and complete the following:
a) $2.5 \times 0.2=2.5 \times \frac{\square}{5}=2.5 \div 5=\square$
b) $2.5 \times 0.2=\frac{\square}{2} \times \frac{\square}{5}=\frac{\square}{\square}=\square$
c) $2.5 \times 0.2=2.5 \times \frac{\square}{10}=2.5 \times \square \div \square$
d) $2.5 \times 0.2=2 \times 0+0.5 \times=+$
5. Find the area of each shape:


c)

0.4 cm
6. Sketch different shapes that have an area of $1 \mathrm{~cm}^{2}$.
7. Calculate the value of each expression when:

| $a b$ | $b^{2}$ | $a^{2}$ | $a^{3}$ | $b^{3}$ |
| :--- | :--- | :--- | :--- | :--- |

a) $a=0.1$ and $b=0.2$
b) $a=0.2$ and $b=0.4$
c) $a=-0.2$ and $b=0.4$
d) $a=-0.2$ and $b=-0.4$

## Questions for depth:

1. Sketch and label an enlargement of the shapes in Q 5 using a scale factor of:
a) 0.5
b) 0.25
c) 0.1
d) 0.8

## Week 8: Fractions 4

## Session 1: Dividing fractions by integers

## Concept Corner

Dividing fractions by integers might be thought of different ways. For example, $\frac{2}{3} \div 2$ can be thought of as:
$\frac{2}{3}$ split into 2 $\qquad$ groups is...
or:

$$
\frac{2}{3} \text { is } 2 \text { of what? }
$$



Using the model, we can see that the answer to both questions is $\qquad$ .

We can also think rewrite this as $\frac{2}{3} \times \frac{1}{2}$ as use multiplication models.

1. Copy and complete the following:
a)

"Twelve is three lots of $\qquad$ _" $12 \div 3=$
b)

"Twelve is two lots of $\qquad$ "
$12 \div 2=$ $\qquad$
c)

"Twelve is one lot of ___" " $12 \div 1=$
2. Find the missing value and write the division:
a)

b)

c)

d)

e)

3. Work out the division calculation linked to the bar model:

a)


$$
\frac{3}{4} \div 3=\frac{a}{a}
$$

b)


$$
\frac{4}{5} \div 2=\frac{\square}{\square}
$$

c)

d)


$$
\frac{2}{5} \div 2=\frac{1}{5}
$$

$\frac{2}{3} \div=\frac{a}{\square}$
$\frac{6}{7} \div-=\frac{\square}{\square}$
4. Draw a bar model and compute the division:
a) $\frac{3}{4} \div 3$
b) $\frac{2}{3} \div 2$
c) $\frac{4}{3} \div 4$
d) $\frac{4}{7} \div 2$
e) $\frac{6}{7} \div 2$
f) $\frac{6}{5} \div 3$
5. Compute the following
a) $\frac{1}{3} \div 3$
b) $\frac{1}{4} \div 2$
c) $\frac{1}{2} \div 3$
e.g.

d) $\frac{2}{3} \div 3$
e) $\frac{3}{4} \div 2$
f) $\frac{5}{2} \div 3$
$\frac{1}{3} \div 2=\frac{2}{6} \div 2=\frac{1}{6}$
6. Each cylinder holds 1 L. If shared equally, how much soda does each person receive?
a)

b)

c)


In which situation do the people receive the most soda?
7. Copy and complete the following:
a) $20 \div 2=20 \times \frac{\square}{\square}$
b) $\frac{4}{5} \div 2=\frac{4}{5} \times \frac{\square}{\square}$
c) $\frac{3}{8} \div 4=\frac{3}{8} \times \frac{\square}{\square}$

Write each of the divisions in Q5 as a product of two numbers.

## Questions for depth:

1. 

a) A group of people share $1 \frac{2}{3} \mathrm{~L}$ of soda, another group shares $2 \frac{5}{6} \mathrm{~L}$. Each person receives the same amount of soda, how many people could be in each group?
b) Change the amount of soda each group shares, can you always find a solution?

## Session 2: Modelling division by fractions I

## Concept Corner

When $\qquad$ a number by a fraction, such as $8 \div \frac{2}{3}$, we can consider that 8 is $\frac{2}{3}$ of the result.

Therefore, $8 \div \frac{2}{3}=$ $\qquad$


1. Write a corresponding division for each sentence:
e.g. Twelve is three lots of $\qquad$ $.12 \div 3=$ ?
a) Ten is five lots of $\qquad$ .
b) Thirty is ten lots of $\qquad$ .
c) Twenty is four groups of $\qquad$ .
d) Eighty is $\qquad$ scaled by a factor of 20 .
2. For each bar model write a matching sentence and division:
e.g. $\square$
" Twelve is half of $\qquad$ " $12 \div \frac{1}{2}=24$
a)

b)

c)

d)

3. Calculate the following and draw your own bar model:
a) $8 \div \frac{1}{5}$
b) $8 \div \frac{2}{5}$
c) $8 \div \frac{4}{5}$
d) $9 \div \frac{3}{4}=$ $\qquad$ e) $9 \div \frac{3}{5}=$ $\qquad$ f) $9 \div \frac{3}{2}$
g) $18 \div \frac{3}{4}=$
h) $27 \div \frac{3}{5}=$
4. Find the missing values for each of the bar models
a)


b)
$\frac{3}{4}$

c)

d)

e)

f)


For each bar model write a matching division and multiplication
e.g. for a)

$$
\frac{3}{4} \div \frac{3}{5}=? \quad \text { and } \quad \frac{3}{4}=\frac{3}{5} \times ?
$$

5. Sketch a diagram to complete the statement
e.g.
 is $\frac{1}{4}$ of

a)

is $\frac{1}{2}$ of $\qquad$
b)

is $\frac{1}{3}$ of $\qquad$
c)

is $\frac{2}{3}$ of $\qquad$
d) $\qquad$
e)
 is $\frac{3}{4}$ of $\qquad$
f)

is $\frac{1}{3}$ of
$\qquad$

For each diagram write a matching division and multiplication
6. Calculate the following and draw your own diagram
a) $\frac{3}{5} \div \frac{3}{4}$
b) $\frac{6}{7} \div \frac{3}{4}$
c) $\frac{6}{5} \div \frac{3}{4}$
d) $\frac{4}{3} \div \frac{2}{5}$
e) $1 \frac{1}{3} \div \frac{4}{5}$
f) $\frac{3}{4} \div \frac{2}{5}$

## Questions for depth:

1. Write equivalent expressions for each of the following:
a) $x \div \frac{1}{5}$
b) $x \div \frac{1}{3}$
c) $x \div \frac{1}{6}$
d) $3 n \div \frac{3}{4}$
e) $3 n \div \frac{3}{5}$
f) $3 n \div \frac{3}{7}$
2. Create your own word problems that match the division calculations in Q6.

## Session 3: Modelling division by fractions II

## Concept Corner

Another way to think about ___ fractions is to consider how many times the $\qquad$ goes in to the dividend.
E.g. $1 \div \frac{1}{4}$ : how many times
 does $\frac{1}{4}$ go in to 1 ? $\qquad$
Using the same technique we can work out that $4 \div$ $\qquad$ $=6$

1. What value is missing each of the following:

"Eight goes into twenty-four $\qquad$ times" $24 \div 8=$

" 9 scaled by a factor of $\qquad$ is 27 "
$27 \div 9=$

"Three goes in to twelve $\qquad$ times" $12 \div 3=$
2. Draw similar diagrams for the following:
a) $6 \div 2$
b) $42 \div 6$
c) $24 \div 8$
3. Use the diagrams to calculate the following:
a)
 is lots of
 $3 \div \frac{1}{2}=$ $\qquad$
b)

$\qquad$ lots of
 $2 \div \frac{1}{3}=$
c)

is lots of
$\frac{1}{2} \div \frac{1}{6}=$

d)

is lots of
ソ'••' $1 \frac{1}{2} \div \frac{1}{6}=\square$
4. Tom drew a diagram that represents: $6 \div \frac{3}{4}$

a) Draw a similar diagram to represent:
i) $2 \div \frac{1}{3}$
ii) $2 \div \frac{2}{3}$
iii) $1 \div \frac{1}{4}$
iv) $3 \div \frac{1}{4}$
b) Work out the value of each calculation.
5. Copy and complete the following:
a)

b)

c)


$$
\frac{1}{6} \div \frac{1}{2}=\square
$$


d)

6. Calculate the following:
a) $\frac{3}{5} \div \frac{1}{5}$
b) $\frac{3}{5} \div \frac{1}{10}$
c) $\frac{6}{10} \div \frac{3}{10}$
d) $\frac{3}{5} \div \frac{3}{10}$
e) $\frac{6}{15} \div \frac{2}{15}$
f) $\frac{2}{5} \div \frac{2}{15}$
g) $\frac{3}{5} \div \frac{4}{5}$
h) $\frac{6}{10} \div \frac{12}{15}$

## Questions for depth:

1. If $\frac{3}{7} \mathrm{~L}$ of paint can cover $1 \mathrm{~m}^{2}$. Complete the following:
a) 3 L of paint can cover $\qquad$
b) 1 L of paint can cover $\qquad$
c) $\frac{3}{4} \mathrm{~L}$ of paint can cover $\qquad$
d) $n \mathrm{~L}$ of paint can cover $\qquad$

## Session 4: Dividing with fraction in mixed contexts

## Concept Corner

We can use fraction $\qquad$ to help us solve problems in different contexts.

For example:


Charlie has lots of eggs and flour, but only 6 bags of sugar.
It takes $\frac{2}{3}$ of a bag of sugar to bake a cake.
How many cakes can he bake?

$$
\begin{aligned}
& \text { How many times does } \frac{2}{3} \\
& \text { go into __? } \\
& 6 \div \frac{2}{3}=- \\
& \text { He can bake } 9 \text { cakes. }
\end{aligned}
$$

1. Decide what fraction of the square is shaded:
a)

b)

c)


Represent the three fractions above in a different way.
2. Harry has drawn two diagrams to illustrate: $9 \div \frac{3}{4}=12$


1

"Three-quarters goes in to nine, twelve times"

"Nine is three-quarters of twelve"

Draw two similar diagrams to illustrate:
a) $3 \div \frac{3}{4}$
b) $4 \div \frac{2}{3}$
c) $4 \div \frac{4}{5}$
3. Draw five rectangles that have an area of $10 \mathrm{~cm}^{2}$ :

$$
10 \mathrm{~cm}^{2}
$$

4. Solve each problem and write the corresponding division:
a) It takes Tom $\frac{1}{4}$ of an hour to ice a cake. How many can he ice in $2 \frac{3}{4}$ hours?
b) Siobhan has mown $\frac{2}{3}$ of the lawn in the garden. She has mown $20 \mathrm{~m}^{2}$ so far. What is the area of the lawn?
c) 1 L of paint covers $\frac{3}{4}$ of a wall, how many litres are needed to cover the wall?
5. Calculate the following:
a) $\frac{2}{3} \div \frac{1}{3}$
b) $\frac{2}{3} \div \frac{1}{6}$
c) $\frac{2}{3} \div \frac{1}{2}$
d) $\frac{2}{3} \div \frac{1}{4}$
e) $\frac{1}{4} \div \frac{1}{4}$
f) $\frac{1}{4} \div \frac{1}{2}$
g) $\frac{1}{4} \div \frac{1}{6}$
h) $\frac{1}{4} \div \frac{1}{3}$
6. Write two word problems matching the calculations in Q2:
e.g. For $9 \div \frac{3}{4}=12$ :
7. "Harry has $£ 9$. If oranges cost 75 p each, how many can he buy?"
8. "Harry has painted three quarters of a wall. He has painted $9 \mathrm{~m}^{2}$ in total, what is the area of the wall?"

## Questions for depth:

1. Using each of the number cards complete:
a)

b)

c)


## Week 9: Fractions 5

## Session 1: Adding and subtracting fractions

## Concept Corner

When fractions are written with a $\qquad$ denominator, we can simply add or $\qquad$ how many parts there are.
E.g. $\qquad$ sevenths add 3 sevenths $=8$ sevenths


$$
\begin{aligned}
& \frac{4}{5}-\frac{3}{5}= \\
& 3 \text { tenths }+1 \text { tenths }=0.3+\ldots=\frac{3}{10}+\frac{1}{10}=\frac{4}{10}
\end{aligned}
$$

1. In the images below, the whole hundred square represents 1 . What are the values of the shaded areas? Write your answers as fractions and decimals. An example has been done for you.
i)


iii)

$0.35 \quad \frac{35}{100}$
iv)



a) Draw your own hundred squares and shade them to represent:
i) 0.8
iii) 0.07
iii) $\frac{13}{100}$
b) Is it possible to represent all of the numbers in part a) together square? Explain your answer.
2. Copy and complete the addition calculations below.
a) $\frac{2}{10}+\frac{}{10}=\frac{7}{10}$
b) $\frac{3}{8}-\frac{2}{8}=\frac{-}{8}$
c) $\frac{7}{15}+\frac{8}{15}=$
d) $\frac{24}{25}=\frac{}{25}+\frac{}{25}$
e) $\frac{3}{7}+\frac{-}{7}=1 \frac{2}{7}$
f) $1 \frac{3}{4}=\frac{-}{4}-\frac{}{4}$
3. Phil is using a hundred square to represent 1 . Look at his statement below.

a) Explain why Phil is wrong.
b) Draw your own hundred square and shade it to correctly represent $0.35+0.06$.
4. Copy and complete the addition calculations below.
a) $\frac{2}{10}+\frac{1}{10}=\frac{}{10}$
b) $\frac{20}{100}-\frac{15}{100}=\frac{}{100}$
c) $\frac{25}{100}+\frac{15}{100}=$
d) $\frac{42}{100}-\frac{25}{100}=\frac{}{100}$
e) $\frac{3}{10}+\frac{17}{100}=\frac{}{100}$
f) $0.32+=0.47$
g) $0.57-\frac{10}{10}=0.47$
h) $\quad=0.57-\frac{4}{100}$
i) $\frac{57}{100}+0.44=$

## Questions for depth:

1. Look at the pattern of growing addition calculations below. If the pattern continues, will there ever be an addition with sum 1?

$$
\frac{1}{100} \longrightarrow \frac{1}{100}+\frac{2}{100} \longrightarrow \frac{1}{100}+\frac{2}{100}+\frac{3}{100} \longrightarrow \frac{1}{100}+\frac{2}{100}+\frac{3}{100}+\frac{4}{100}
$$

2. What values of $n$ will give a pattern where a sum of 1 will occur?


## Session 2: Different denominators

## Concept Corner

Using our understanding of $\qquad$ we can make sensible statements about addition of fractions.


It is helpful to draw diagrams such as $\qquad$ lines to make sense of the size of fractions and their sums.

1. Put the fractions below into ascending order.
$\frac{2}{3}$
$\frac{2}{5}$
$\frac{1}{3}$
$\frac{1}{2}$
$\frac{1}{5}$
2. In the diagrams below each rectangular grid represents 1.

The grids have been shaded to show fraction additions.
Write out the addition each grid shows, an example has been done for you.


b)



e)

3. Look at your answers to question 2 . Which of the additi have an answer that is less than 1? Explain how you k
4. Decide if the inequalities are true or false and explain how you know.
a) $1>\frac{1}{2}+\frac{1}{4}$
b) $\frac{2}{3}+\frac{1}{2}>1$
c) $\frac{1}{2}+\frac{1}{3}>\frac{1}{3}+\frac{1}{3}$
d) $\frac{1}{4}+\frac{1}{2}<\frac{1}{3}+\frac{1}{2}$
e) $\frac{2}{3}+\frac{1}{2}<\frac{3}{4}+\frac{1}{2}$
f) $\frac{2}{3}>\frac{1}{2}+\frac{1}{4}$
5. Look at the number line and inequalities below.


Write a possible value for $\boldsymbol{x}$ if:
a) $y=\frac{1}{2}$
b) $y=\frac{2}{3}$
c) $y=\frac{1}{4}$

## Questions for depth:

1. Look at the number line, inequalities and equation below.

a) If $\boldsymbol{a}=\frac{\mathbf{5}}{\mathbf{6}}$, write down a set of possible values for $\boldsymbol{b}, \boldsymbol{c}$ and $\boldsymbol{d}$.
b) If $\boldsymbol{b}=\frac{2}{3}$, write down a set of possible values for $\boldsymbol{a}, \boldsymbol{c}$ and $\boldsymbol{d}$.
c) If $\boldsymbol{c}=\frac{1}{3}$, write down a set of possible values for $\boldsymbol{a}, \boldsymbol{b}$ and $\boldsymbol{d}$.
d) If $\boldsymbol{d}=\frac{1}{5}$, write down a set of possible values for $\boldsymbol{a}, \boldsymbol{b}$ and $\boldsymbol{c}$.

## Session 3: Using common denominators

Concept Corner
We can accurately add or subtract any


Using this diagram we can see that $\frac{1}{6}$ and $\frac{1}{16}$ can both be $\qquad$ in the form $\frac{x}{48}$.

$$
\frac{1}{6}+\frac{1}{16}=\frac{8}{48}+\frac{3}{48}=
$$

1. Copy and complete the sets of equivalent fractions.
a) $\frac{2}{3}=\frac{-}{9}=\frac{}{12}$
b) $\frac{-}{5}=\frac{4}{20}=\frac{4}{10}$
c) $\frac{2}{7}=\frac{}{21}=\frac{4}{}$
d) $\frac{30}{}=\frac{10}{8}=1 \frac{-}{4}$
e) $\frac{84}{}=\frac{7}{11}=\frac{}{33}$
f) $\frac{84}{}=\frac{7}{11}=\frac{}{33}$
2. Copy and complete the fraction calculations below
a) $\frac{1}{2}+\frac{1}{4}=\frac{-}{4}+\frac{1}{4}=$
b) $\frac{1}{4}+\frac{1}{8}=\frac{-}{8}+\frac{}{8}=$
c) $\frac{2}{3}-\frac{1}{6}=\frac{-}{6}-\frac{1}{6}=$
d) $\frac{3}{4}+\frac{5}{12}=\frac{-}{12}+\frac{5}{12}=$
3. In the diagram below, the whole rectangular grid represents 1.


Which student do you agree with? Explain your answer.
4. Look at the rectangular grid in question 3.
a) What is the answer to the fraction addition represented in question 3 ?
b) Draw your own 24 -square rectangular grids representing 1, and shade them in to represent and work out the answer to these fraction calculations:
i) $\frac{1}{3}+\frac{5}{8}=$
ii) $\frac{5}{12}+\frac{3}{8}=$
iii) $\frac{7}{8}-\frac{5}{6}=$
5.
a) Find the lowest common multiples of the following pairs of numbers.
i) 8 and 10
ii) 12 and 3
iii) 7 and 4
b) Complete the fractions calculations below. Your answers to 5a) might help.
i) $\frac{5}{8}+\frac{3}{10}=$
ii) $\frac{11}{12}-\frac{2}{3}=$
iii) $\frac{2}{7}-\frac{3}{4}=$
c) Explain the connections between your answers to 5a) and your methods of calculation in 5b)
6. Look at the number line below. Complete each calculation in two different ways (not using equivalent fractions).

a) $\frac{5}{8}+\cdots=$ a number between $a$ and $b$
b) $\frac{7}{5}+=$ a number between $b$ and $c$
c) $\frac{20}{7}=$ a number between $c$ and $d$

## Questions for depth:

1. Look at the number line below.


Write down two different sets of values for $w-z$ such that

## Session 4: Distributivity

## Concept Corner

We can use our understanding of $\qquad$ to help
$\qquad$ fraction calculations.

For example:

$$
\frac{3}{8} \times 7+\frac{1}{8} \times 7=\left(\frac{3}{8}+\ldots\right) \times 7=\frac{1}{2} \times 7
$$



$$
3 \times \frac{2}{3}-3 \times \frac{1}{6}=\left(--\frac{1}{6}\right) \times 3=\frac{1}{2} \times 3
$$

1. Copy can complete the following calculations.
a) $\frac{2}{3}-\frac{1}{6}=$
b) $=\frac{3}{5}+\frac{1}{2}$
c) $\frac{5}{6}+=\frac{11}{12}$
d) $\frac{5}{3}-\frac{11}{15}=$
e) $\frac{1}{6}=-\frac{2}{9}$
f) $\frac{4}{9}+\frac{2}{5}=$
2. Copy and complete the calculations below:
a) $\frac{2}{3} \times 7+\frac{1}{5} \times 7=(\ldots+\ldots) \times 7$
b) $\frac{2}{7} \times 3-3 \times \frac{1}{4}=3 \times(\ldots-\ldots)$
c) $8 \times \ldots-\frac{1}{9} \times 8=\ldots \times\left(\frac{3}{5}-\frac{1}{9}\right)$
d) $\frac{7}{12} \times 10-10 \times \frac{1}{1}=5$
3. Decide if each of the statements below are true or false:
e) $\frac{2}{3} \times 3+\frac{1}{4} \times 3>3$
f) $\frac{4}{3} \times 12-12 \times \frac{1}{4}>12$
g) $8 \times \frac{2}{3}-\frac{1}{4} \times 8>4$
h) $\frac{3}{5} \times 10-10 \times \frac{1}{6}>5$
4. Match the cards showing equivalent calculations.
$\frac{1}{2} \times 5-5 \times \frac{3}{4}$
$5 \times \frac{1}{4}$

$\frac{5}{2}+\frac{1}{4}$
$5 \times \frac{1}{2}-\frac{1}{4} \times 5$
$\frac{1}{2} \times 5+\frac{1}{4}$
$5 \times\left(\frac{1}{2}-\frac{3}{4}\right)$

$$
\frac{1}{2} \times 5+\frac{1}{4} \times 5
$$

5. Work out the answer to each pair of cards from question 3.
6. The cards below show the area of each shape. Match then to the correct shape.

7. Work out an expression to calculate the area of each shape below. Leave your answers in the form $\times b$ or similar.


$b$| $\frac{4}{5}$ |  |
| :---: | :---: |
| $\frac{1}{2}$ |  |
|  |  |

## Questions for depth

1. Draw two different hexagons similar to those in quest
area of $\frac{7 b}{8}$.

## Week 10: Percentage

## Session 1: Percentage number line

## Concept Corner

We can represent fractions as $\qquad$ .

Percentage is another way of writing numbers as fractions with a $\qquad$ of 100 .

We can show these percentages on a
$\qquad$ line as in the example below.


1. Copy the number line below and place the numbers shown onto it.

2. Write the numbers below in percentage form.
a) $\frac{1}{4}$
b) 0.5
c) 0.8
d) $\frac{3}{10}$
e) 0.15
f) $\frac{3}{4}$
g) $\frac{2}{5}$
h) $\frac{3}{2}$
3. Write down two different numbers that lie between $\frac{1}{2}$ and $40 \%$.
4. Write your answers to question 3 in a different form ( decimal).
5. Write down the numbers missing from the boxes on the number lines in fraction, percentage and decimal form.

b)

6. Write down the number that is halfway between:
a) $\frac{1}{4}$ and $75 \%$
b) 0.8 and $100 \%$
c) $\frac{4}{5}$ and $120 \%$
d) 0.5 and $\frac{9}{10}$
e) $140 \%$ and $\frac{7}{10}$
f) 0.1 and $100 \%$
7. Place the numbers below into the two groups shown.


## Questions for depth:

1. Decide if the fractions below are greater than or less than $55 \%$. Explain how you know.
$\frac{11}{21}$

$\frac{11}{201}$
$\frac{12}{21}$
2. Place the four numbers from question 1 above in ascending order.
3. Look at your list of numbers from question 2 above. Wr
percentage form that lie between the numbers in ascending order.

## Session 2: Tenths, hundredths and thousandths

## Concept Corner

Tenths, hundredths and $\qquad$ can be written in different ways, including as $\qquad$

| Fractions | Decimal | Percent |
| :---: | :---: | :---: |
| $-\cdots \frac{3}{10}+\frac{1}{100}+\frac{235}{1000}$ | 0.235 |  |



We can also represent these numbers using a number line.


1. The 100 -squares below each represent 1 .

What numbers are represented by the shaded sections. Write your answers as fractions, decimals and percentage.
a)

b)

c)

2. The 100 -square below represents 1 .

Look at the two students' statement. Do you agree with either of the students?
Explain why or why not.

3. Look at the table below. The first row has been completed as an example. Copy and complete the remainder of the table.

| Fraction | Different <br> equivalent <br> fraction | Sum of tenths, <br> hundredths and <br> thousandths | Decimal | Percentage |
| :---: | :---: | :---: | :---: | :---: |
| $\frac{3}{5}$ | $\frac{60}{100}$ | $\frac{6}{10}+\frac{0}{100}+\frac{0}{1000}$ | 0.6 | $60 \%$ |
|  |  | $\frac{1}{10}+\frac{0}{100}+\frac{5}{1000}$ |  |  |
| $\frac{13}{20}$ |  |  |  | $12.5 \%$ |
|  | $\frac{918}{1000}$ | $\frac{0}{10}+\frac{3}{100}+\frac{7}{1000}$ |  |  |
|  |  |  |  |  |

4. The images below show a 'zoomed in' view of part of a number line. Write down the numbers that lie at points A-D as shown.

5. Write your answers to question 4. as percentages.

## Questions for depth:

1. Complete the number cards below to form numbers that lie between D and E in question 4 above.
$\square$

2. Put your answers to question 1 in ascending order.

## Session 3: Converting fractions and percentage

## Concept Corner

We can convert between fractions and percentages using our understanding of $\qquad$ fractions.

$$
\frac{3}{5}=\frac{\square}{100}=60 \%
$$

$$
45 \%=\frac{45}{}=\frac{9}{}
$$



Some fractions have recurring or repeating $\qquad$ digits when written as a percentage or decimal. E.g.:

$$
\frac{1}{=}=0.33 \dot{3}=33 . \dot{3} \%
$$

1. Write the fractions below as percentages.
a) $\frac{3}{4}$
b) $\frac{1}{5}$
c) $\frac{7}{20}$
d) $\frac{23}{50}$
e) $\frac{7}{10}$
f) $\frac{107}{100}$
g) $\frac{24}{25}$
h) $\frac{12}{40}$
i) $\frac{2}{3}$
j) $\frac{11}{10}$
k) $\frac{545}{1000}$
1) $\frac{7}{5}$
2. Write the percentages below as fractions in their simplest form.
a) $30 \%$
b) $80 \%$
c) $85 \%$
d) $45 \%$
e) $12 \%$
f) $66 . \dot{6} \%$
g) $125 \%$
h) $120 \%$
3. Match each fraction card with a percentage card. Complete the cards where necessary.

$25 \%$
4. Put the fraction cards from question 3 in descending o
5. One student is trying to explain their approach for writing $\frac{3}{5}$ in percentage form. Draw a diagram (e.g. a bar model) to help explain.

6. Decide if the statements below are true or false.
a) $\frac{9}{4}=225 \%$
b) $\frac{15}{4}=400 \%$
c) $\frac{5}{3}>200 \%$
d) $\frac{10}{3}>300 \%$
e) $\frac{7}{5}>200 \%$
f) $\frac{9}{5}>200 \%$
7. Decide if the numbers in each box are the same or different. Explain how you know.
a)



## Questions for depth:

1. How many solutions to question 8 are there if you can only use each digit card once?
2. How many solutions to question 8 are there if you only have the number cards 0,1 , $2,3,5,6$ and can use them only once each?

## Session 4: Percentages of quantities I

## Concept Corner

We can use our understanding of $\qquad$ to help calculate with percentages.

The example below shows a set of $\qquad$ calculations and statements.
$75 \%$ of $£ 150$


$\frac{3}{4} \times £ 150$

1. Write the percentages below as fractions in their simplest form:
a) $50 \%$
b) $10 \%$
c) $40 \%$
d) $65 \%$
e) $15 \%$
f) $12.5 \%$
2. Calculate:
a) $30 \%$ of $£ 50$
b) $60 \%$ of 150 cm
c) $85 \%$ of 250 kg
3. Match each bar model to a calculation. Complete the bar models and calculations.

$40 \%$ of $120=$ $\qquad$ $66.6 \%$ of $72=$ $\qquad$ $37.5 \%$ of $\_=63$
$75 \%$ of $300=$
4. Re-write the calculation cards from question 2 as fraction calculations. E.g.:

5. Look at Phil's statement below. Explain why he is wrong. You can draw a diagram to help.

6. Find the odd one out in each set below. Explain how you know it doesn't fit the set.
a)

b)

$$
40 \% \times 60 \quad 20 \% \text { of } 120 \quad 80 \% \times 40
$$

c)

$$
62.5 \% \times n \quad \frac{3}{8} \text { of } n \quad \frac{625}{100} \times n
$$

7. Match up the pairs of equivalent calculations from the cards below.

$0.75 \times 132$
$200 \% \times 49$
8. Complete the equations below
a) $20 \% \times 15 \%=$ $\qquad$ \% of 0.05
b) $\frac{1}{3} \times 15 \%=\ldots \%$ of $\frac{1}{6}$
c) $87.5 \% \times \frac{8}{7}=\frac{4}{3} \times \ldots \%$
d) $0.6 \times \ldots=\frac{1}{5}$ of $\qquad$

## Questions for depth:

1. Write the following expressions in the form $\boldsymbol{a} \%$ of $\boldsymbol{n}$.

$$
\left(\frac{1}{2}\right)^{2} \times 0.5 \times 3 n
$$

$$
\left(\frac{2}{5}\right)^{2} \times\left(\frac{1}{2}\right)^{3} \times n
$$

$$
\underline{3}^{3} \quad \underline{1} \quad \underline{n}
$$

